

Energy Bands In Solid

Formation of Energy band in Semiconductors

Most of Semiconductors has Crystalline form

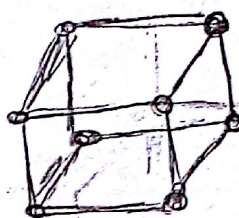
e.g. Cubic crystal

- Simple Cubic
- Body centered Cubic
- Face Centered Cubic

A) Simple Cubic lattice

→ There are 8 atoms in Corners

→ each atom is shared with 8 unit cells



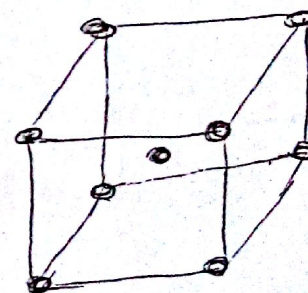
Watch a Video in Youtube if you don't understand the shape

∴ No. of atoms per unit cell = $8 \cdot \frac{1}{8} = 1$ atom

B) Body Centered Cubic lattice

→ 8 Atoms in Corners

+ one atom inside unit cell



→ No. of atoms per unit cell

$$= (8 \cdot \frac{1}{8}) + 1 = 2 \text{ atoms}$$

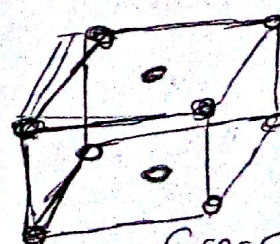
C) Face Centered Cubic lattice

→ Cubic has 6 Faces

→ each Face contain atom

→ each atom is shared between 2 unit cell

+ 8 Atoms in Corner



□

$$\hookrightarrow \text{No. of atoms per unit cell} = (6 \cdot \frac{1}{2}) + (8 \cdot \frac{1}{8})$$

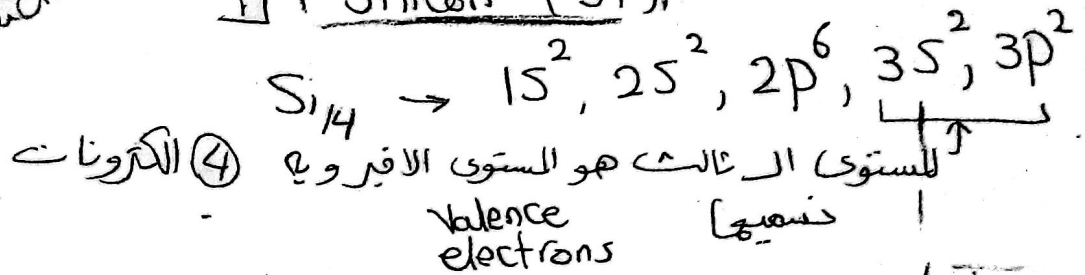
$$= 3 + 1 = 4 \text{ atoms}$$

Valence Electrons الالكترونات التكافؤ

Ex. of Semiconductors : "Most used semiconductor in optoelectronics"

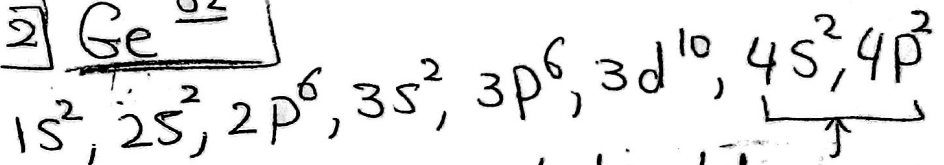
Just to Remember
Semiconductors

1 Silicon (Si)



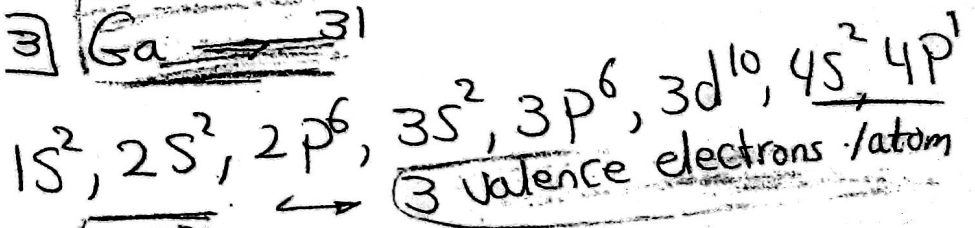
Si has 4 valence electron / atom

2 Ge ³²

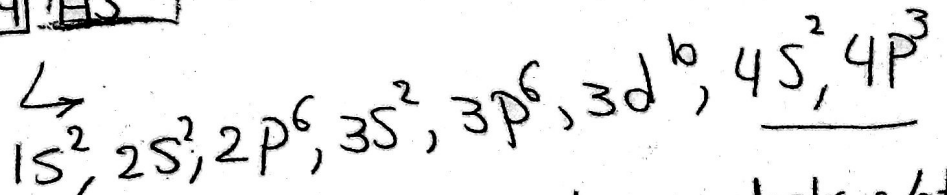


Ge has 4 valence electron / atom

3 Ga ³¹



4 As ³³



As has 5- valence electrons / atom

Q (7)

Calculate an avg. number for the valence electrons per unit volume in Semiconductor crystals?

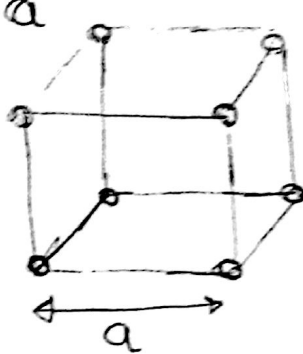
~Sol~

- ① Calculate Volume of unit cell
- ② Calculate atoms / unit cell
- ③ Estimate no. of electrons / unit volume

↳ For simplicity Let's take Simple Cubic lattice.

④ Interatomic Space = a

① ∴ Volume of simple cubic
 $= a^3$



In Semiconductors $a = 3-7 \text{ \AA}$
 assume $a = 5 \text{ \AA}$

Semiconductor Crystal

- ↳ SC → ✓
- ↳ BCC
- ↳ FCC

∴ Volume of unit cell $= (5)^3 = 125 \text{ \AA}^3 = 125$
 $= 125 \times 10^{-24} \text{ cm}^3$

$1 \text{ \AA} \rightarrow 10^{-10} \text{ m}$
 $1 \text{ \AA} \rightarrow 10^{-8} \text{ cm}$

② Atoms / unit cell
 $= 8 \cdot \frac{1}{8} = 1 \text{ atom}$

③ No. of atoms / unit volume $= \frac{1}{125 \times 10^{-24}} = 0.8 \times 10^{+22}$
 cm^{-3}

④ Valence electrons / atom $\approx 4 \text{ electrons / atom}$

⑤ ~~Electron~~ Avg. no. of valence electrons / unit volume
 $= 0.8 \times 10^{+22} \times 4 = 3.2 \times 10^{+22}$
 electron / cm^3

Note
 +ve → Very Large
 Sign no.

→ $\approx 10^{+22} \rightarrow 10^{+23} \text{ electrons / cm}^3$

3

Energy Bands in Solids

1] Solid is state of matter

↓ Collection of atoms

+ve nuclear

To study Behaviour of electrons → -ve charged electrons

↓
Schrodinger eqn.

Schrodinger eqn.

$$\frac{\partial^2 \psi}{\partial x^2} = -\frac{2m}{\hbar^2} (E - U) \psi$$

$$\frac{\partial^2 \psi}{\partial x^2} + \frac{2m}{\hbar^2} (E - U) \psi = 0$$

Total energy → this is eigen value of this eqn.

ψ → دالة لوانت لها القيمة
الايه متفرقة كما في
موضع في قيم القوية

eigen value

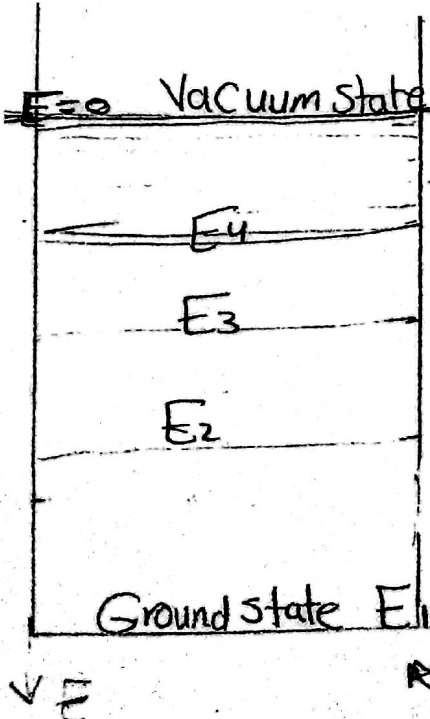
IF we take isolated atom

e.g] Hydrogen atom

"Simple atom has one electron"

Schrodinger eqn.

When we solve for this atom.



We found that E is quantized "discrete" (n) discrete

$$E_n = \frac{-m e^4}{8 \epsilon_0^2 h^2} \cdot \frac{1}{n^2}$$

$$E_n = -\frac{13.6}{n^2} \text{ eV}$$

n = 1, 2, 3, ...

discrete

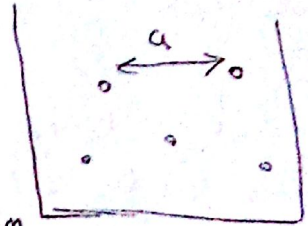
E

Isolated Atom Can be characterized by discrete Energy Level.

← (Note) (In gas)

interatomic ~~between~~

$$= 100 \text{ \AA} \rightarrow 1 \text{ Mm}$$



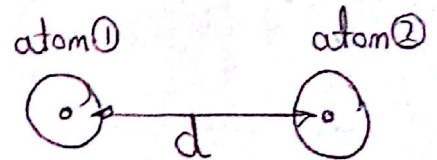
But

← In Semiconductors $a = 5 \text{ \AA}$

← When d is large

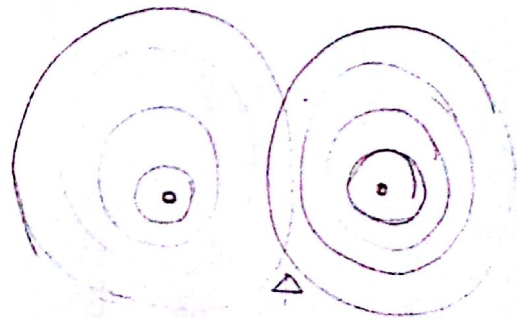
we can consider each atom is isolated

atom \rightarrow so energy band will be discrete



← When d is small

عندما تقترب الذرات من بعضها قليلاً يحدث Split "انفصال" لـ Energy state
2-Energy state (أي)



Outer energy level will split

لو تقارب عدد كبير من الذرات يحدث splitting للـ energy state
مكون energy Band

الذي يتأثر به energy state الخارجى وليست القريبة من النواة

E_3 _____

E_2 _____

E_1 _____

Ground state \uparrow
 ψ

هذا هو الحال لو تقاربنا ذراتنا فقط

For Reading

Pauli Exclusion principle

صبدأ بولي للاستبعاد

If two or more atoms are brought together, their outer (i.e. valence) energy level must be split so they will be different from one another

بنفس
المبدأ

في فيزياء ثانوية عامة

صبدأ بولي:

في ذرة ما لا يوجد
الكثرونات لها نفس
اعداد الكم الاربعة

لذلك لا كنت بقول

~~3s²~~

في الكثرونيت في 3s

3s 1 1

بقول ان فيه الكثرون
بيور مع عقارب الساعة
و (آخر عكسها)

2s

1s 1 atom

2 atoms

2 atoms

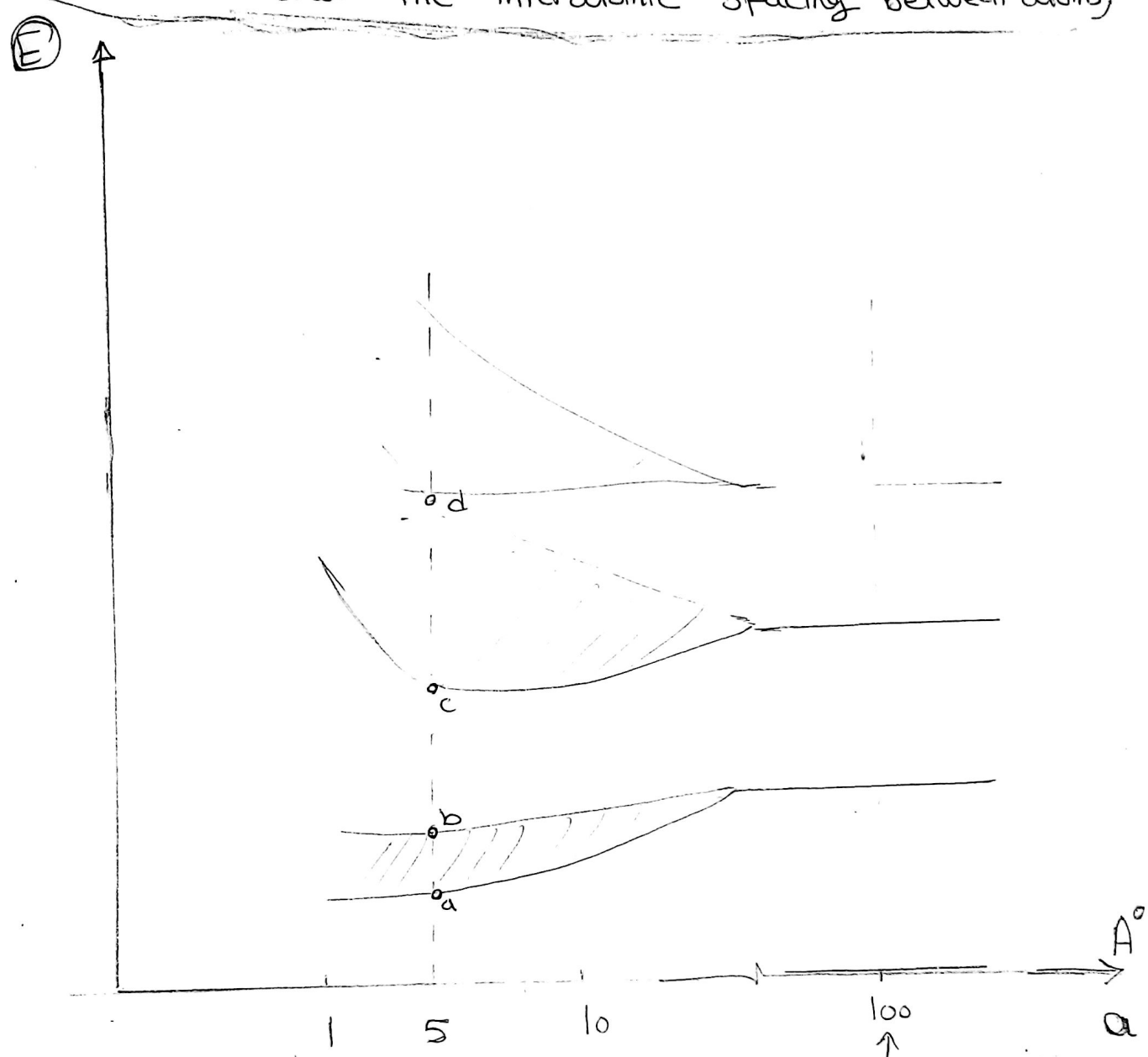
2 atoms

N atoms

N atoms

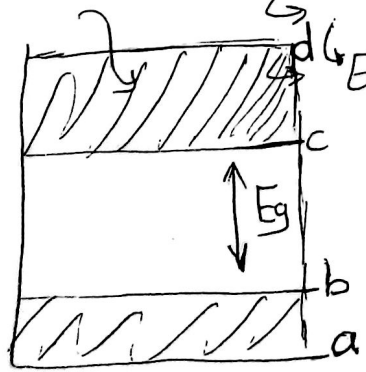
N atoms

Q.8 Draw a relation between Atom energy and the interatomic spacing between atoms



Band Diagram

Conduction Band



→ Semi Conductor

→ 10^{22} atom/cm³

→ $a \approx 5 A^0$

Energy level is not discrete

← Valence Band

interatomic space like in gas
isolated atoms
"E → discrete"

Q(2)

$$\hookrightarrow E = E_k + E_p$$

Sec (2)

$$E = \frac{1}{2}mv^2 + \left(\frac{-e^2}{4\pi\epsilon_0 r} \right) \rightarrow \textcircled{I}$$

for finding only

out target \rightarrow to get $v \rightarrow$ as function of \textcircled{I}
 $r \rightarrow$ as function of \textcircled{I}

\hookrightarrow Solution of Schrodinger eqn. :

$$\psi(x) = e^{jkx}$$

this function is periodic every \textcircled{L}



$$\psi(x) = \psi(x+L)$$

$$e^{jkx} = e^{jkx} \cdot e^{jKL}$$

$$\therefore KL = n(2\pi)$$

$$n = 1, 2, 3, \dots$$

$$K = \frac{2\pi n}{L} \rightarrow K \text{ is quantized}$$

حيث الدائرة $\therefore L = 2\pi r \Rightarrow \boxed{K = \frac{n}{r}}$

$$\therefore \boxed{r = \frac{n}{K}} \rightarrow \textcircled{1}$$

\hookrightarrow De-Broglie Relation

$$P = \frac{h}{\lambda}$$

$$= \frac{h}{2\pi} \cdot \frac{2\pi}{\lambda}$$

$$P = \hbar K = \hbar \frac{n}{r}$$

$$P \cdot r = \hbar \cdot n$$

$$mvr = \hbar n$$

$$\therefore V = \frac{h n}{m r} \rightarrow (2)$$

\hookrightarrow Coulomb's Force

$$F_c = \frac{e^2}{4\pi\epsilon_0 r^2} \rightarrow (3)$$

$$\& F = m \cdot a = m \cdot \frac{v^2}{r} \rightarrow (4)$$

From (3) & (4)

$$\therefore \frac{e^2}{4\pi\epsilon_0 r^2} = m \cdot \frac{v^2}{r}$$

$$v^2 = \frac{e^2}{4\pi\epsilon_0 r \cdot m} = \frac{e^2}{4\pi\epsilon_0 m \cdot r} \rightarrow (5)$$

~~Square of~~ Eqn. (2) power (2)

$$\therefore v^2 = \frac{h^2 n^2}{m^2 r^2}$$

$$\therefore \frac{e^2}{4\pi\epsilon_0 m r} = \frac{h^2 n^2}{m^2 r^2} \quad h^2$$

$$\therefore r = \frac{h^2 n^2 \cdot 4\pi\epsilon_0}{m e^2} = \left(\frac{h^2}{4\pi^2} \right) \frac{n^2 \cdot 4\pi\epsilon_0}{m e^2}$$

$$\therefore \boxed{r = \frac{h^2 n^2 \epsilon_0}{\pi m e^2}} \rightarrow (6) \quad \sim r \text{ as function of } n$$

From 6 \rightarrow into (2)

$$\therefore \boxed{V = \frac{h}{2\pi} \cdot \frac{n}{m} \cdot \frac{\pi m e^2}{h^2 n^2 \epsilon_0} = \frac{e^2}{2 h n \epsilon_0}} \rightarrow (7)$$

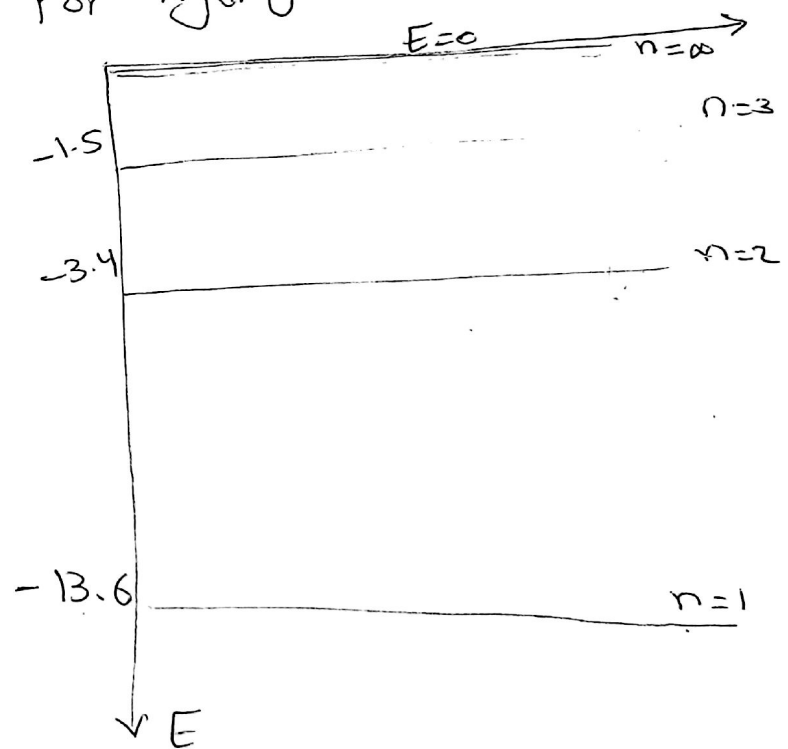
$$\infty E_K = \frac{1}{2} m v^2 = \frac{e^4 m}{8 h^2 n^2 \epsilon_0^2} \rightarrow \textcircled{\text{II}}$$

$$E_P = \frac{-e^2}{4 \epsilon_0^2 h^2 n^2} \rightarrow \textcircled{\text{III}}$$

From $\textcircled{\text{II}}$ & $\textcircled{\text{III}}$ into $\textcircled{\text{I}}$

$$\infty E = \frac{-e^4 m}{8 h^2 n^2 \epsilon_0^2} = \frac{-13.6 \text{ eV}}{n^2}$$

For hydrogen



$$\textcircled{\text{C}} E_{\text{photon}} = E_2 - E_1 = -3.4 - (-13.6) = 10.2 \text{ eV}$$